

Towards uniform point distribution in feature-preserving point cloud filtering

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Abstract While a popular representation of 3D data, point clouds may contain noise and need filtering before use. Existing point cloud filtering methods either cannot preserve sharp features or result in uneven point distributions in the filtered output. To address this problem, this paper introduces a point cloud filtering method that considers both point distribution and feature preservation during filtering. The key idea is to incorporate a repulsion term with a data term in energy minimization. The repulsion term is responsible for the point distribution, while the data term aims to approximate the noisy surfaces while preserving geometric features. This method is capable of handling models with fine-scale features and sharp features. Extensive experiments show that our method quickly yields good results with relatively uniform point distribution.

Keywords point cloud filtering; point distribution; feature preservation

1 Introduction

Researchers have made remarkable progress in point cloud filtering in recent years. Recent methods typically aim to maintain sharp features in the original point cloud while projecting the noisy points to

the underlying surfaces. The filtered point cloud data can then be used for upsampling [1], surface reconstruction [2, 3], skeleton learning [4, 5], computer animation [6, 7], etc.

Existing point cloud filtering methods can be divided into traditional and deep learning techniques. In the traditional class, position-based methods [8–10] obtain good smoothing results, while normal-based methods [3, 11] better maintain sharp edges of models (e.g., CAD models). Some of these methods incorporate repulsion terms to prevent points from aggregating but still leave gaps near the edges of geometric features, which affects reconstruction quality. Deep learning-based approaches [12–14] require a number of noisy point clouds with ground-truth models for training and often achieve good denoising results through a proper number of iterations. These methods are usually based on local information, and lead to uneven point distribution in the filtered results even in the presence of a repulsion loss term. It is difficult for such methods to handle unevenly distributed and sparsely sampled point clouds since it is difficult to automatically adjust the patch size. Different patch sizes in the point cloud also pose a significant challenge to the learning procedure.

The above analysis motivates us to produce filtered point clouds which preserve sharp features yet have a relatively uniform point distribution. Given a noisy point cloud with normals as input, we first smooth the input normals using bilateral filtering [1]. Principal component analysis (PCA) [15] is used for the initial estimation of normals. Secondly, we update the point positions in a local manner by reformulating an objective function consisting of an edge-aware data term and a repulsion term inspired by Refs. [11, 16]. The two aim to preserve geometric features and provide uniform point distribution,

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respectively. Output with these properties is obtained after a few iterations. We have conducted extensive experiments to compare our approach to various other approaches, including position- and normal-based approaches, both learning and traditional. The results demonstrate that our method outperforms state-of-the-art methods in most cases, both visually and quantitatively.

2 Related work

In this paper, we only review the most relevant work to our research, including traditional point cloud filtering and deep learning-based point cloud filtering.

2.1 Traditional point cloud filtering

2.1.1 Position-based methods

LOP was first proposed in Ref. [8]. It is a parameterization-free method and does not rely on normal estimation. Besides fitting the original model, a density repulsion term was added to evenly control the point cloud distribution. WLOP [9] provided a novel repulsion term to solve the problem that the original repulsion function in LOP drops too quickly as the support radius increases. The filtered points are distributed more evenly by WLOP. EAR [1] added an anisotropic weighting function to WLOP to smooth the model while preserving sharp features. CLOP [10] is another LOP-based approach; it redefines the data term as a continuous representation of a set of input points.

Although only based on point positions, these approaches achieve reasonable smoothing results. However, as they disregard normal information, these approaches tend to smear sharp features such as sharp edges and corners.

2.1.2 Normal-based methods

FLOP [17] adds normal information to the novel feature-preserving projection operator and preserves features well. Meanwhile, a new kernel density estimate (KDE)-based random sampling method was proposed for accelerating FLOP. Moving least squares (MLS)-based approaches [18, 19] have also been applied to point cloud filtering; they rely upon the assumption that the given set of points implicitly define a surface. In Ref. [20], the authors presented an algorithm that allocated an MLS local reference domain for each point that most suited its adjacent points and further projected the points

to the underlying plane. This approach uses the eigenvectors of a weighted covariance matrix to obtain normals when the input point cloud has no normal information. APSS [21], RMLS [22], and RIMLS [3] use this idea. RIMLS is based on robust local kernel regression and gives better results when noise is high. GPF [11] incorporates normal information in a Gaussian mixture model (GMM) with two terms, and preserves sharp features well. A robust normal estimation method was proposed in Ref. [16] for both point clouds and meshes using a low-rank matrix approximation algorithm, where an application of point cloud filtering was demonstrated. To keep the geometric features, Ref. [23] first filters the normals using discrete operators defined on point clouds, and uses a bi-tensor voting scheme for the feature detection step.

Inspired by image denoising, researchers have also investigated use of non-local data in point cloud denoising. Non-local-based point cloud filtering methods [24–27] often incorporate normal information and use various similarity definitions to update point positions in a non-local manner. Thus, Ref. [24] proposes a similarity descriptor for point cloud patches based on MLS surfaces. Ref. [25] designs a height vector field to describe the difference between the neighborhood of the point with neighborhoods of other points on the surface. Inspired by the low-dimensional manifold model, Ref. [26] extends it from image patches to point cloud surface patches, which serves as a similarity descriptor for non-local patches. Ref. [27] presents a new multi-patch collaborative method that regards denoising as a low-rank matrix recovery problem. They define the given patch as a rotation-invariant height-map patch and denoise the points by imposing a graph constraint.

Filtering methods that rely on normal information usually yield good results, especially for point clouds with sharp features. However, these methods strongly depend on the quality of the input normals, and poor normal estimates may lead to poor filtering results.

Our proposed approach falls in the normal-based category. Inspired by GPF, we estimate normals of the input point cloud using bilateral filtering [1] to get high-quality normal information. Note that if the input point cloud only contains positional information, PCA is used to compute the initial

normals. The point positions are then updated in a local manner using the bilaterally filtered normals [16]. We also add a repulsion term [16] to ensure a more uniform distribution of the filtered points.

2.2 Deep learning point cloud filtering

A variety of deep learning-based methods have emerged for dealing with noisy point clouds [12, 14, 28–32]. For point cloud filtering, PointProNets [13] introduced a novel generative neural network architecture that encodes geometric features in a local way and efficiently obtains an underlying surface. However, the generated underlying surface suffers from holes due to the input shapes. NPD [30] redesigned the framework on the basis of PointNet [33] to estimate normals from noisy shapes and then projected the noisy points to the predicted reference planes. Another PointNet-inspired method is called Pointfilter [14]. It starts from points and learns the displacement between the predicted points and the raw input points. Moreover, this approach requires normals only in the training phase. In the testing phase, only point positions are taken as input to obtain filtered shapes with feature-preserving effects. EC-NET [31] presented an edge-aware network (similar to PU-NET [34]) for connecting edges of the original points. This method retains sharp edges of 3D shapes well, but the training stage requires manual labeling of edges. Inspired by PCPNet [35], PointCleanNet [12] developed a data-driven method for both classifying outliers and reducing noise in raw point clouds. A novel feature-preserving normal estimation method was designed in Ref. [32] for point cloud filtering while

preserving geometric features. Deep learning-based filtering methods usually yield good results more automatically, for point clouds with high density. However, low-density input may lead to poor filtering outcomes. Also, such methods require sufficient suitable samples for training.

3 Method

3.1 Overview

Our approach has two phases. In phase one, we smooth the initial normals using bilateral filtering, following Ref. [1], to ensure the quality of normals. In phase two, we update point positions with the smoothed normals to obtain a uniformly distributed point cloud preserving geometric features. Figure 1 overviews the proposed approach. We now explain the second phase in detail.

3.2 Position update

We define the noisy input with M points to be $P = \{\mathbf{p}_i\}_{i=1}^M$, $\mathbf{p}_i \in R^3$, with corresponding filtered normals $N = \{\mathbf{n}_i\}_{i=1}^M$, $\mathbf{n}_i \in R^3$. To obtain local information from a given point \mathbf{p}_i , we define a local structure \mathbf{s}_i for each point in the point cloud, consisting of the k nearest points to the current point. We employ an edge-aware recovery algorithm [16] to obtain filtered points by minimizing

$$\mathcal{D}(P, N) = \sum_i \sum_{j \in \mathbf{s}_i} |(\mathbf{p}_i - \mathbf{p}_j) \mathbf{n}_j^T|^2 + |(\mathbf{p}_i - \mathbf{p}_j) \mathbf{n}_i^T|^2 \quad (1)$$

where \mathbf{p}_i is the point to be updated and \mathbf{p}_j is some neighboring point in the corresponding set \mathbf{s}_i . Eq. (1) essentially adjusts the angles between the tangent

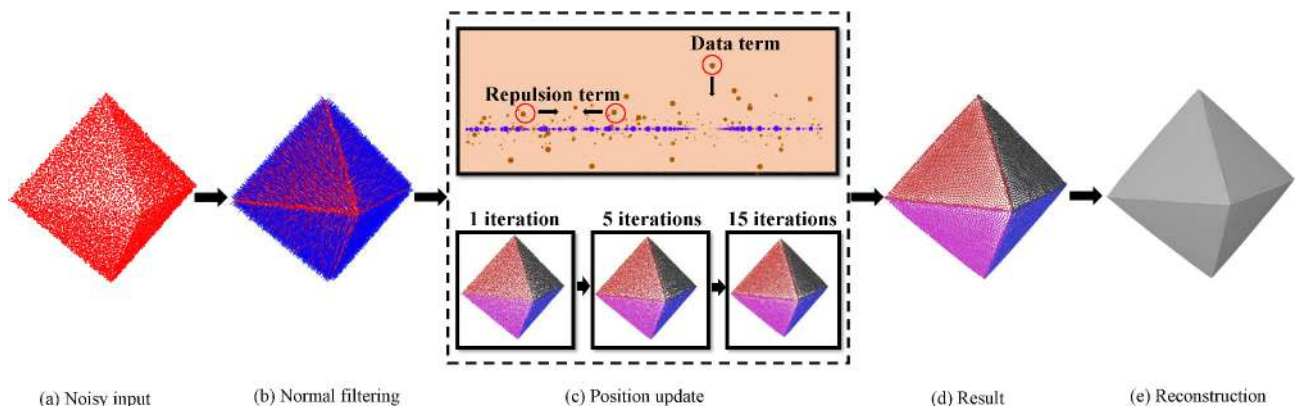


Fig. 1 Approach. (a) Noisy input. Red points are corrupted with noise. (b) Filtered normals. Blue lines are filtered results of the initial normals. (c) Position update method, using a data term for feature preservation and a repulsion term for uniform distribution. Multiple iterations are performed to achieve a better filtered result. (d) Filtered point cloud. (e) Mesh reconstructed from (d).

vector formed by \mathbf{p}_i and \mathbf{p}_j and the corresponding normal vectors $\mathbf{n}_i, \mathbf{n}_j$, respectively.

Figure 2 demonstrates how the points are updated on an assumed local plane by this edge-aware technique. It can be seen that the quality of the filtered points depends heavily on the quality of the estimated normals. Our normals are generated by bilaterally filtering the original input normals, given the simplicity and effectiveness of this approach.

3.3 Repulsive force

From Fig. 3, it can be seen that points move towards sharp edges during the position update step, resulting in gaps near sharp edges. It is demonstrated in Ref. [16] that minimizing $\mathcal{D}(P, N)$ inevitably yields gaps near sharp edges; the gaps in the filtered points can greatly impact downstream applications such as upsampling and surface reconstruction. Thus, we introduce a repulsion force $\mathcal{R}(P, N)$ based on both point coordinates and normals [11] to better control the distribution of points:

$$\mathcal{R}(P, N) = \sum_i \lambda_i \sum_{j \in s_i}^M \eta(r_{ij}) \theta(r_{ij}) \quad (2)$$

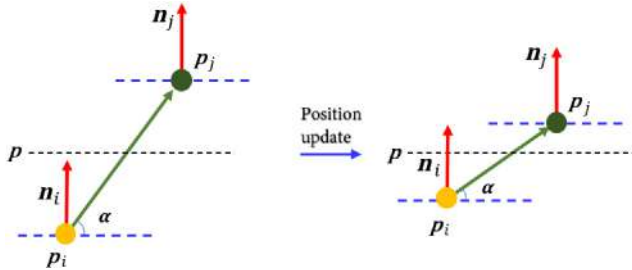


Fig. 2 Left: original points. Right: updated points. \mathbf{p}_i and \mathbf{p}_j are the current point and a neighboring point respectively. \mathbf{n}_i and \mathbf{n}_j are the normals of \mathbf{p}_i and \mathbf{p}_j , respectively. A local plane surface is assumed.

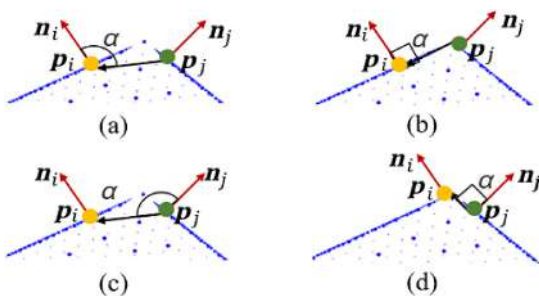


Fig. 3 Movement of the filtered points around sharp edges. Blue points: underlying surface. Yellow, green points: two neighboring points that need to be moved. (a, b) Movement of \mathbf{p}_j with fixed \mathbf{p}_i . (c, d) Movement of \mathbf{p}_i with fixed \mathbf{p}_j . Note how points move towards the sharp edges and concentrate there, leading to gaps around the sharp edges.

where $r_{ij} = \|(\mathbf{p}_i - \mathbf{p}_j) - (\mathbf{p}_i - \mathbf{p}_j) \mathbf{n}_j^T \mathbf{n}_j\|$, $\eta(r) = -r$, and $\theta(r) = \exp(-r^2/(h/2)^2)$ is a smoothly decaying weight function.

3.4 Minimization

Combining Eq. (1) and Eq. (2), our final position update optimization problem is to find

$$A = \underset{P}{\operatorname{argmin}} \mathcal{D}(P, N) + \mathcal{R}(P, N) \quad (3)$$

We employ the gradient descent method to do so and obtain each updated point \mathbf{p}'_i . The partial derivative of Eq. (3) with respect to \mathbf{p}_i is

$$\frac{\partial A}{\partial \mathbf{p}_i} = \sum_{j \in s_i} \frac{(\mathbf{n}_j \mathbf{p}_i^T - \mathbf{n}_j \mathbf{p}_j^T) (\mathbf{p}_i \mathbf{n}_j^T - \mathbf{p}_j \mathbf{n}_j^T)}{\partial \mathbf{p}_i} + \frac{\lambda_i \beta_{ij} (\mathbf{p}_i - \mathbf{p}_j) (\mathbf{I} - \mathbf{n}_j^T \mathbf{n}_j)}{\partial \mathbf{p}_i} \quad (4)$$

where \mathbf{I} is a 3×3 identity matrix, and

$$\beta_{ij} = \frac{\theta(r_{ij})}{r_{ij}} \left| \frac{\partial \eta(r_{ij})}{\partial r} \right| \quad (5)$$

The updated point \mathbf{p}'_i can thus be calculated by

$$\mathbf{p}'_i = \mathbf{p}_i + \gamma_i \sum_{j \in s_i} (\mathbf{p}_j - \mathbf{p}_i) (\mathbf{n}_j^T \mathbf{n}_j + \mathbf{n}_i^T \mathbf{n}_i) + \mu \frac{\sum_{j \in s_i} w_j \beta_{ij} (\mathbf{p}_i - \mathbf{p}_j) (\mathbf{I} - \mathbf{n}_j^T \mathbf{n}_j)}{\sum_{j \in s_i} w_j \beta_{ij}} \quad (6)$$

where γ_i is set to $1/(3|s_i|)$ following Ref. [16], $w_j = 1 + \sum_{j \in s_i} \theta(\|\mathbf{p}_i - \mathbf{p}_j\|)$, and μ is a parameter which controls the relative magnitude of the repulsive force.

3.5 Algorithm

The proposed method is described in Algorithm 1. We first filter the normals using bilateral filtering. By feeding the filtered normals and raw point positions into Algorithm 1, we obtain the updated point positions. Depending on the number of points in the model and the noise level, we accordingly choose k used to generate the local patches and the number

Algorithm 1 Point cloud filtering algorithm

Input: Noisy point set P , with corresponding filtered normals N , neighborhood size k , number of iterations t , repulsion strength μ

Output: Uniformly distributed set of filtered points P' for t iterations **do**

for each point \mathbf{p}_i **do**

 construct a local patch s_i from k nearest neighbors
 update point position via Eq. (6)

end for

end for

of iterations to perform. Table 1 lists the parameter settings used for various models in the experiments.

Table 1 Parameter settings for various models

Parameter	k	μ	t
Figure 4	30	0.3	5
Figure 5	30	0.3	5
Figure 6	30	0.3	5
Figure 7	30	0.3	3
Figure 8	30	0.3	5
Figure 9	30	0.3	5
Figure 10	30	0.3	10
Figure 11	30	0.3	5
Figure 12	30	0.3	5

4 Experiments

4.1 Settings

The proposed method was implemented in Visual Studio 2017 and executed on a PC with an Intel i9-9750h CPU and NVidia RTX2070 GPU.

4.2 Parameter settings

The parameters to be chosen are the local neighborhood size k , the coefficient of repulsion force μ , and the number of iterations t . As the number of points affects the range of neighbors significantly, in order to find the appropriate k for different models, we determined the value of k in the range [15, 45] ($k = 30$ by default) according to the number of points in each model. To make the distribution of points more even while preserving features, we use the parameter μ to balance the magnitude of the repulsive force between points and t to control the number of iterations. Usually, for models with relatively smooth surfaces, we set a relatively larger μ and a lower t , and for models with sharp surfaces, we set a relatively smaller μ with a higher number of iterations to obtain the filtered points. Table 1 gives the parameters used for each model considered in the experiments.

4.3 Methods compared and approach

The proposed method was compared to state-of-the-art techniques including a non-deep learning position-based method CLOP [10], non-deep learning normal-based methods GPF [11] and RIMLS [3], and deep learning-based methods TotalDenoising (TD) [36], PointCleanNet (PCN) [12], and Pointfilter (PF) [14]. We employ the following approach to ensure a fair comparison. (a) We first normalized and centralized

the noisy input. (b) As GPF and RIMLS require high-quality normals, we used the same bilateral filter [1] in each case to provide the same input normals for each model. (c) We tuned the main parameters of each method as well as we could, to produce the best final visual results. (d) For the deep learning-based methods, we used the results of the 6th iteration for TD and iterate three times for both PCN and PF. (e) For visual comparisons, we used EAR [1] for upsampling to provide a similar number of points for each method when visualizing a given model. For surface reconstruction, we adopted the same parameters for each given model.

4.4 Evaluation metrics

We used two common evaluation metrics to quantitatively analyze the results. Let the ground-truth point cloud and the filtered point cloud be respectively defined as $S_1 = \{\mathbf{x}_i\}_{i=1}^{|S_1|}$, $S_2 = \{\mathbf{y}_i\}_{i=1}^{|S_2|}$. Note that the numbers of ground-truth points $|S_1|$ and filtered points $|S_2|$ may differ slightly. The metrics are *chamfer distance*:

$$e_{\text{CD}}(S_1, S_2) = \frac{1}{|S_1|} \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2^2 + \frac{1}{|S_2|} \sum_{y \in S_2} \min_{x \in S_1} \|y - x\|_2^2 \quad (7)$$

and *mean square error*:

$$e_{\text{MSE}}(S_1, S_2) = \frac{1}{|S_1| |\text{NN}(y)|} \sum_{x \in S_1} \sum_{y \in \text{NN}(y)} \|x - y\|_2^2 \quad (8)$$

where $\text{NN}(y)$ denotes the nearest neighbors in S_1 to point y in S_2 . Here we set $|\text{NN}(y)| = 10$ following Ref. [14], i.e., we search for 10 nearest neighbors for each point y in the predicted point set S_2 .

4.5 Visual comparisons

4.5.1 Point clouds with synthetic noise

To show the denoising effects of our method, we conducted experiments on models with synthetic Gaussian noise at levels of 0.5% and 1.0%. Compared to other state-of-the-art methods, our visual results outperform them both in terms of smoothing and feature preservation. The results benefit from the fact that the position update considers normal information and distributes the filtered points more evenly.

We may also observe the traits of other methods in the experiments. CLOP always obtains good results in terms of smoothing. However, since it is

a position-based method, it may blur sharp features. While GPF adds a gap-filling step after projecting the points onto the underlying surface, it still finds it difficult to maintain a uniform distribution, especially for points near sharp edges. This method may also sharpen less sharp features. RIMLS yields promising results in both noise removal and feature preservation. However, its filtered points are often unevenly distributed, which affects the performance of downstream applications such as upsampling and surface reconstruction.

The learning-based method TD also yields good smoothing results, but it does not seem to maintain the fine features of the model well. PCN typically produces less sharp features, while PCN does not provide good smoothing given a relatively high level

of noise. PF does not need normal information at run time, and achieves good feature-preserving effects while denoising. However, when the noisy points are sparse, this method cannot extract needed information from the sparse point cloud, leading to distortion of the filtered points.

Since normal information is taken into account in our method, it can keep sharp features well. Importantly, the greater uniformity of its point distribution makes it stand out in point cloud filtering and downstream applications like upsampling and surface reconstruction.

The top rows of Figs. 4–6, readily show that our method provides the most uniform point distribution. Figures 5, 6, and 8 give upsampling results for three different models after filtering. As shown below in

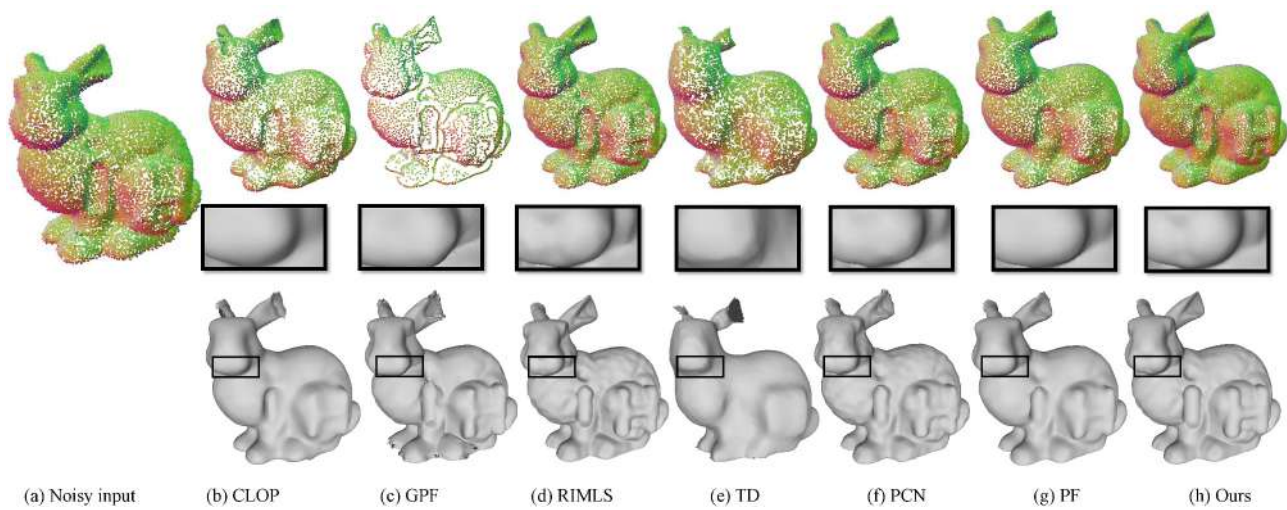


Fig. 4 Above: results on the Bunnyhi model corrupted with 0.5% synthetic noise. Below: surface reconstruction results.

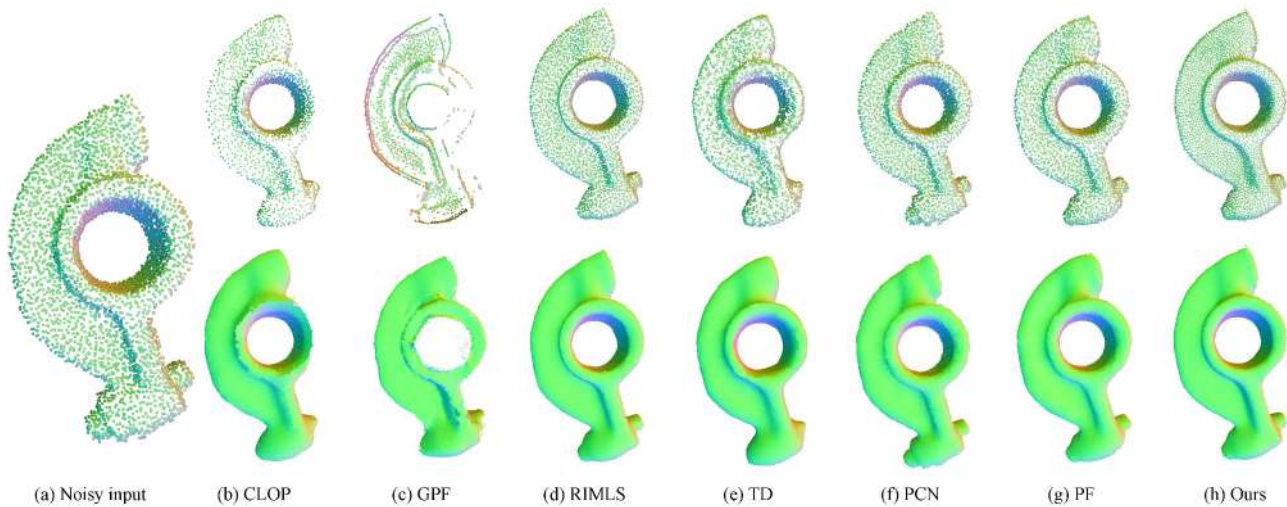


Fig. 5 Above: results on Rockerarm corrupted with 0.5% synthetic noise. Below: corresponding upsampling results.

Figs. 5 and 6, sharp edges are maintained well during denoising. The enlargement in Fig. 8 also shows the effect of our filtering method, where the shapes of the kitten’s ears are well maintained . Results of surface reconstruction are presented in Figs. 4 and 7. As

the enlargement shows, the bunny’s mouth and nose in Fig. 4 are well maintained. Figure 7 also shows filtered results for our method on a simple geometric model with sharp edges. Our method is best in terms of maintaining details and sharp edges.

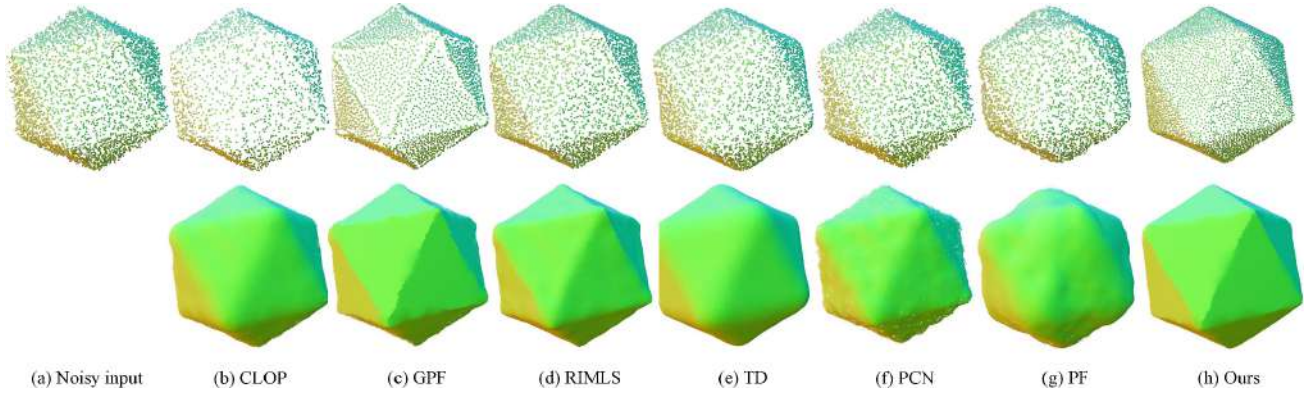


Fig. 6 Above: results on Icosahedron corrupted with 1.0% synthetic noise. Below: corresponding upsampling results.

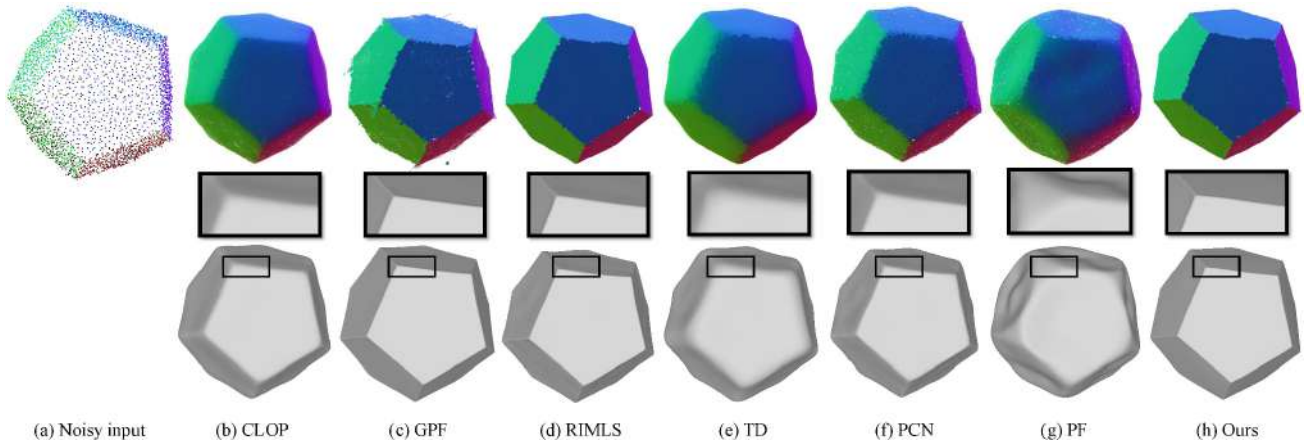


Fig. 7 Results on Dodecahedron corrupted with 0.5% synthetic noise. Above: corresponding upsampling results. Below: reconstructed meshes.

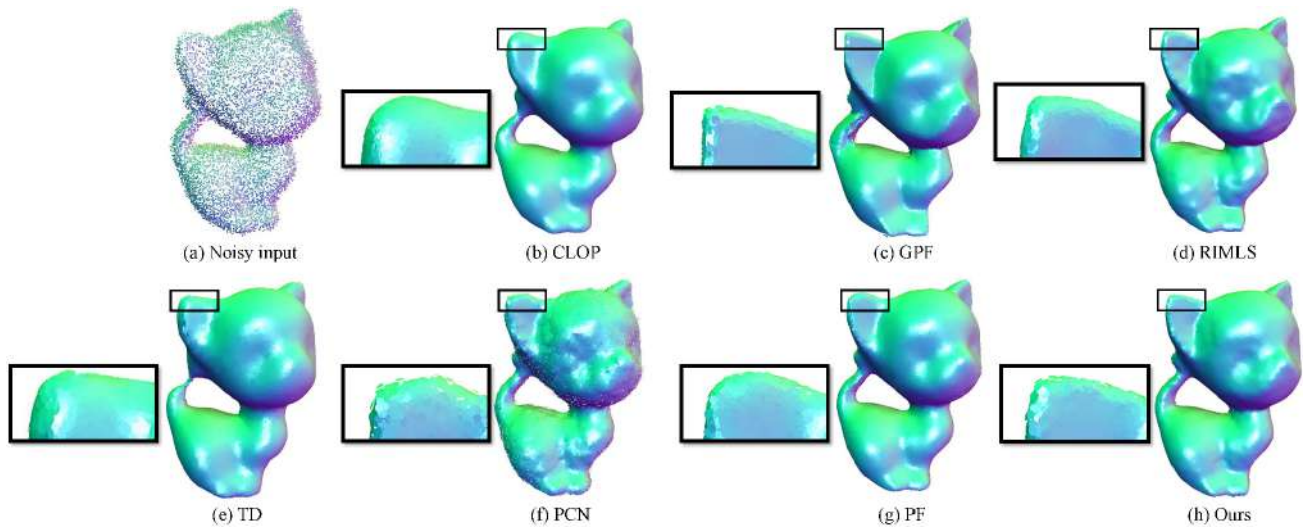


Fig. 8 Upsampling results on Kitten corrupted with 1.0% synthetic noise.

4.5.2 Point clouds with raw scanner noise

In addition to using synthetic noise, we also performed experiments on raw scanned point clouds. Results for our method and existing methods are given in Figs. 9–12. The filtered results in Fig. 9 show that our method performs best in terms of smoothing and preserving

details. As can be seen from the enlargement, most methods blur the mouth of the model or even lose it after denoising. Note that although the model we use here has the same shape as one used in Ref. [14], the filtered results may differ since our sample points were sparser than theirs.

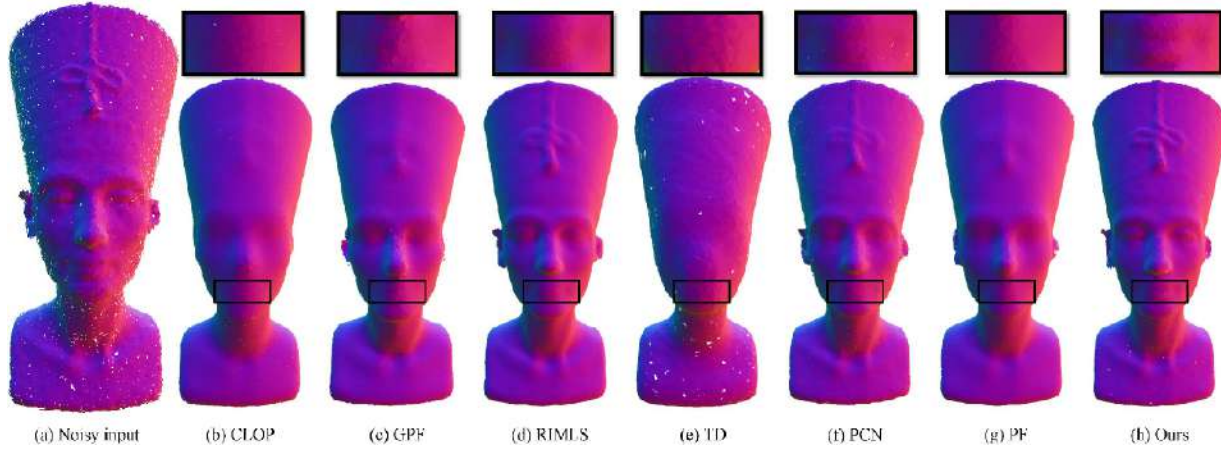


Fig. 9 Upsampling results on the Nefertiti raw scanned model.

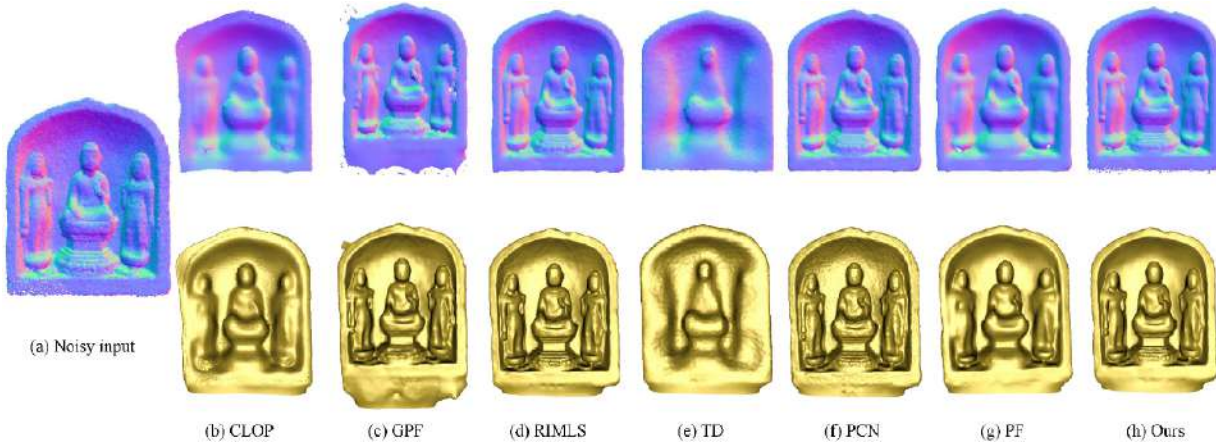


Fig. 10 Results on BuddhaStele raw scanned model. Above: corresponding upsampling results. Below: reconstructed meshes.

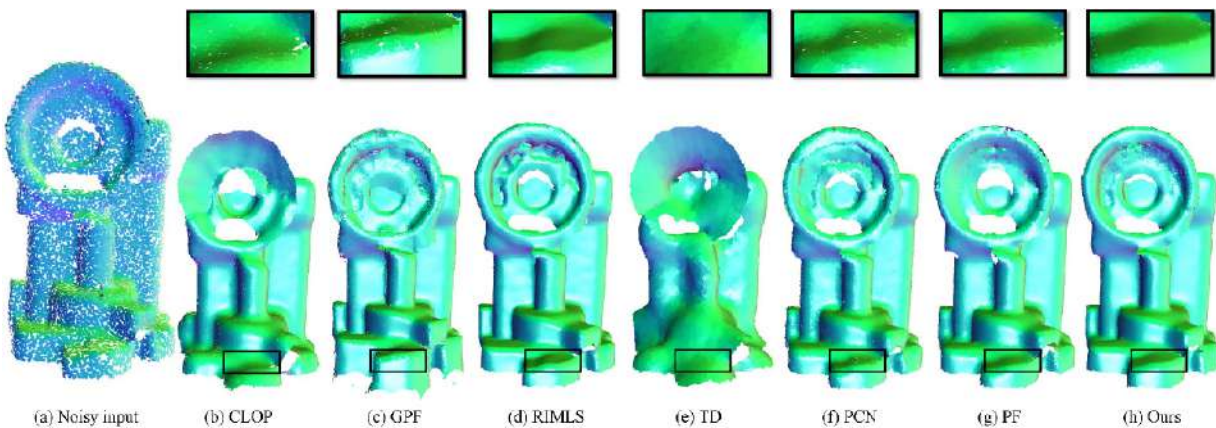


Fig. 11 Upsampling results on the Realscan raw scanned model.

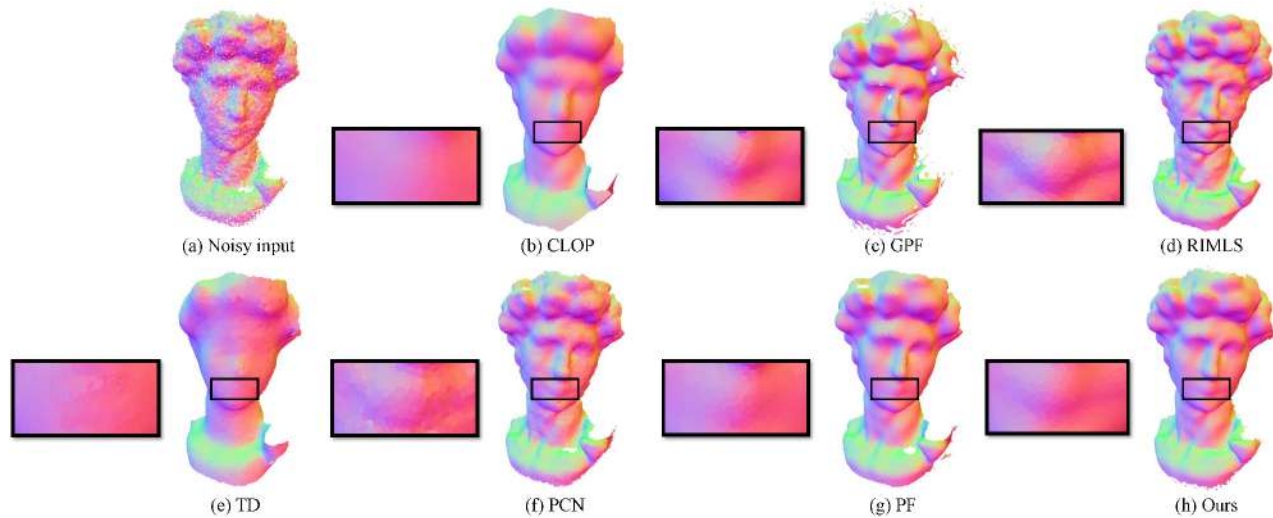


Fig. 12 Upsampling results on the David raw scanned model.

Figure 10 shows the filtered results on the BuddhaStele raw scanned model. Results after upsampling are shown above; below are results after surface reconstruction using the screened Poisson method [2]. From details such as the steps in the model, it can be seen that our method again outperforms the other methods. In Fig. 11, our method again maintains sharp edges well. As the enlargement shows, other state-of-the-art methods either distort sharp edges or smooth them. Figure 12 shows filtered results on the David raw scanned model. Our method preserves features better during filtering, and as the enlargement shows, our approach maintains facial features better than other methods.

4.6 Quantitative comparisons

We also make a quantitative comparison using the two evaluation metrics given earlier. As there is no corresponding ground-truth model for the raw scanned point clouds, we used the models with synthetic noise for evaluation. Results using the Chamfer Distance metric are given in Table 2. Despite the fact that deep learning-based methods are trained on a large number of point clouds, our method still outperforms all deep learning-based methods and indeed achieves the best quantitative result in most cases. In terms of the other evaluation metric mean square error (MSE), our method still outperforms most deep learning methods and again provides the lowest quantitative error in most cases, as shown in Table 3.

These quantitative results are consistent with the visual results, demonstrating that our method

Table 2 Quantitative evaluation of methods on the synthetic point clouds in Figs. 4–8. Deep learning methods are indicated by *. Metric used is Chamfer Distance ($\times 10^{-5}$). The best method for each model is highlighted in bold

Method	Figure 4	Figure 5	Figure 6	Figure 7	Figure 8	Avg.
CLOP [10]	7.84	25.35	26.46	23.83	6.73	16.70
GPF [11]	16.19	31.85	21.52	18.35	15.54	17.58
RIMLS [3]	3.72	5.22	15.70	10.98	4.16	7.12
TD* [36]	23.88	13.20	24.43	19.22	11.86	16.15
PCN* [12]	4.76	6.38	29.87	14.96	6.24	11.18
PF* [14]	4.01	6.63	33.38	30.60	3.68	14.93
Ours	3.11	5.48	12.26	8.14	3.18	5.80

Table 3 Quantitative evaluation of methods on the synthetic point clouds in Figs. 4–8. Deep learning methods are indicated by *. Metric used is MSE ($\times 10^{-3}$). The best method for each model is highlighted in bold

Method	Figure 4	Figure 5	Figure 6	Figure 7	Figure 8	Avg.
CLOP [10]	10.32	13.91	21.86	23.31	9.88	15.86
GPF [11]	11.64	17.07	22.43	23.88	11.97	17.40
RIMLS [3]	10.05	14.02	21.68	23.30	10.02	15.81
TD* [36]	13.22	14.78	22.44	23.36	11.45	17.05
PCN* [12]	10.30	14.28	23.68	23.79	10.59	16.53
PF* [14]	10.02	14.17	23.71	25.28	9.82	16.60
Ours	9.92	14.01	21.46	23.15	9.92	15.69

generally outperforms existing methods both visually and quantitatively. We believe this is because our method provides a more uniform distribution of the filtered points and can handle both sparsely and densely sampled point clouds. In the case of sparse sampling, some deep learning-based methods are unable to obtain meaningful local geometric information from the sparse local neighboring points.

It is also worth noting that although RIMLS achieves comparable visual results to our method in some cases, its numerical errors are greater than those for our method in most cases due to its uneven point cloud distribution.

4.7 Parameter values

We now consider settings for the various parameters. We performed experiments on a point cloud containing 7682 points using different values of k . Figure 13 shows that the best value of k is 30, which we use as the default value for this parameter. It is clear that the best k depends strongly on the density of the point cloud. Using a fixed value of k , when the model has sparse points, the locality determined by k is larger, which may lead to an excessive range that should not be treated as local information, resulting in poor outcome. For point clouds with denser distribution, the size of the neighborhood for the same k becomes smaller, meaning that the k neighborhood contains only a smaller amount of very local information, leading to an uneven distribution of the point cloud. Generally, we use a larger k for denser point clouds to ensure an appropriate number of local neighbors.

As μ is related to the number of iterations t , we give filtered results for different values of μ for various numbers of iterations. Figure 14 demonstrates the filtered point clouds obtained for different μ values when $t = 30$ and $k = 30$. We can see from this figure that as μ increases, the distribution of the point cloud becomes more uniform, but making μ too large makes the model chaotic again. Figure 14(b) shows the filtered results using a low value of μ when

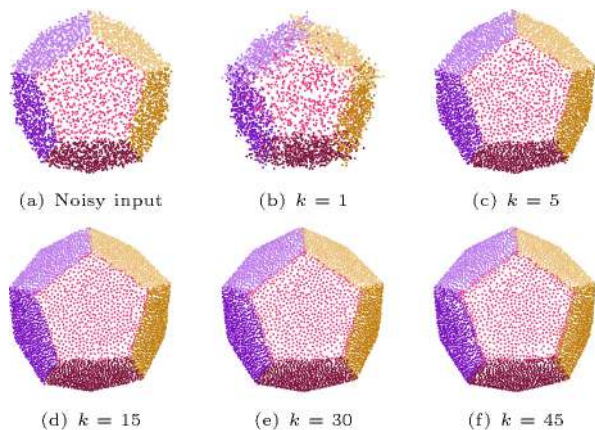


Fig. 13 Filtered results for different k . Noise level: 1.0%, $t = 30$, $\mu = 0.3$.

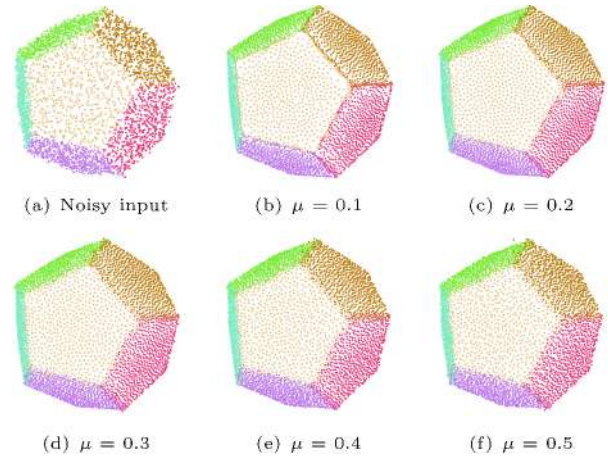


Fig. 14 Filtered results for different μ . Noise level: 1.0%, $t = 30$, $k = 30$.

$i = 30$ and $k = 30$. As we can see, a smaller μ better maintains the edges of the model.

We also conducted experiments using different numbers of iterations. Figure 15 shows that with increasing iterations, the distribution of the filtered point cloud becomes more uniform. However, Fig. 15(d) shows that if too many iterations are used, the boundary of the model becomes unclear again.

4.8 Repulsion term

Local-based filtering approaches tend to converge in certain places when updating the positions. Obviously, this will make downstream applications such as surface reconstruction very difficult. Our method adopts the repulsion term mentioned in Section 3 to evenly distribute the points while filtering, thus improving the quality of the filtered point cloud. As Fig. 16(a) shows, without the repulsion term, it is clear that some points are concentrated at edges, whereas the distribution in Fig. 16(b) is more even.

4.9 Point density

Results under different point densities were also tested. Figure 17 shows that our method yields

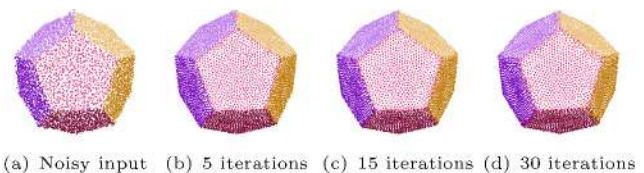


Fig. 15 Filtered results for different number of iterations. Noise level: 1.0%, $k = 30$, $\mu = 0.3$.

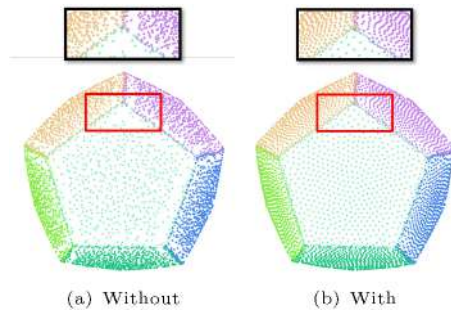


Fig. 16 Filtered results without and with the repulsion term.

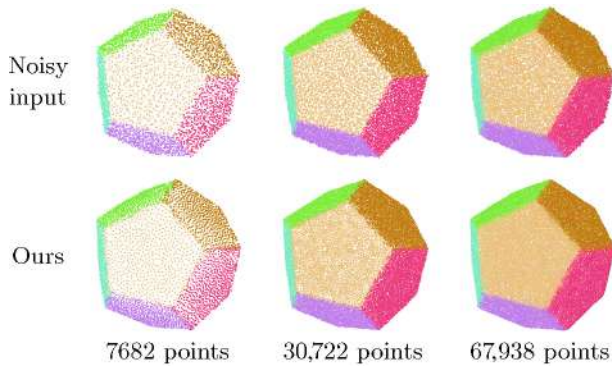


Fig. 17 Filtered results for models with different numbers of sample points.

promising results for both sparse and dense point clouds. As our method requires only local information, for point clouds with greater point density, a desired filtered result can be obtained by setting a larger k .

4.10 Noise level

Different noise levels were applied to the same model to verify the robustness of our approach. Figure 18 gives the filtered results by our method under noise levels of 0.5%, 1.0%, 1.5%, 2.0%, 2.5%, and 3.0%. It can be seen that our method is capable of handling models with different levels of noise but may work less well given excessively high noise. As our method relies

on the quality of normals, it is difficult to accurately keep geometric features if the model has inaccurate normals caused by high noise levels.

4.11 Irregular sampling

We conducted further experiments on models with irregular sampling. Figure 19 provides a visual comparisons of results on an unevenly sampled model for PCN [12], PF [14], and our method. It can be seen that the filtered point cloud from PCN still contains obvious noise while PF blurs the detail features. Our method smooths the model better while preserving features.

4.12 Hole filling

Taking a cube as an example, we experimented on a model with holes. Figure 20 shows the filtered results for different holes. Our method is capable of filling relatively small holes because we consider the distribution of the updated points. However, it is challenging to fill big holes that severely disrupt the surfaces of the model.

4.13 Comparison to Lowrank

Figure 21 compares results of our approach to those of Lowrank [16]. It demonstrates that our method results in a more uniform point distribution than Lowrank when removing noise.

4.14 Indoor scenes

We performed an experiment on the more challenging indoor scene data shown in Fig. 22. The result shows that our method can also deal with point cloud indoor scenes.

4.15 Runtime

Most examples in this paper were completed within 7 s. The most time-demanding was the object in

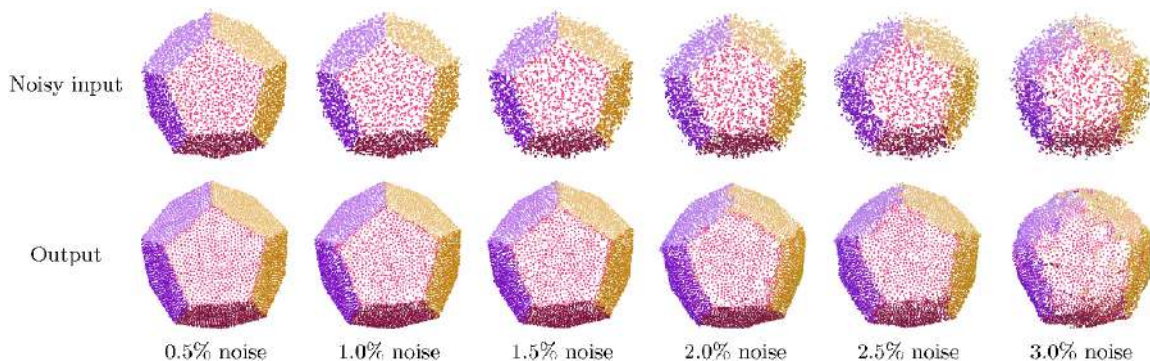


Fig. 18 Filtered results for models with different levels of noise.

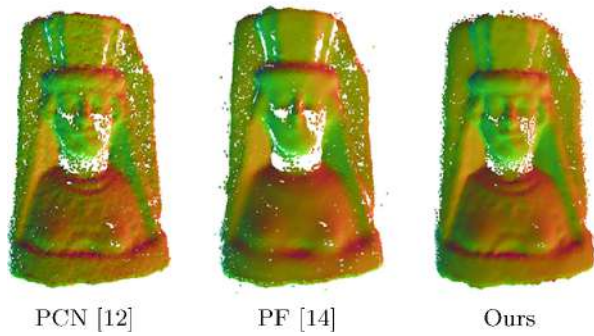


Fig. 19 Filtered results for an irregularly sampled point cloud.

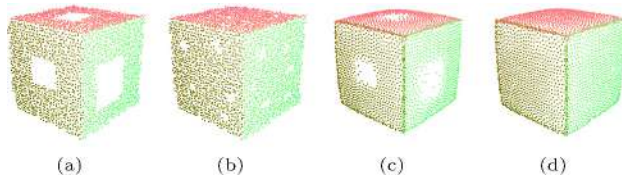


Fig. 20 Filtered results with various holes. (a) Input cube with large holes. (b) Input cube with small holes. (c) Output after filtering (a). (d) Output after filtering (b).

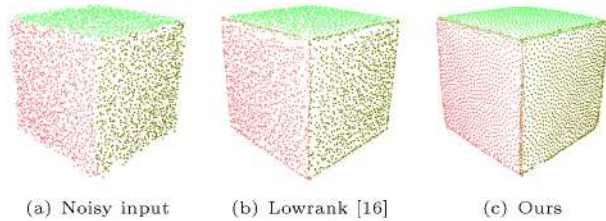


Fig. 21 Filtered points of ours and Lowrank [16].

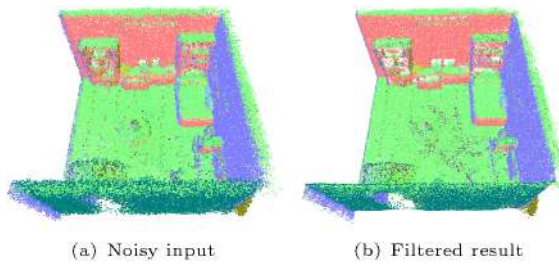


Fig. 22 Filtered result on noisy point cloud of an indoor scene.

Fig. 11, taking 28 s.

Running time for the proposed method was measured for different k and numbers of iterations. Table 4 shows that as k and the number of iterations increase, the runtime increases accordingly.

In each iteration, our method gathers k neighbors

Table 4 Runtime (s) on Dodecahedron for different k and numbers of iterations t

Numbers of iterations	$t = 5$	$t = 15$	$t = 30$	$t = 60$
$k = 30$	1.41	3.77	7.37	14.69
$k = 60$	2.33	6.37	12.36	24.36

for each point. Thus the larger k is, the longer the computation takes. The number of iterations also has a similar effect on the run time. However, since our method is locally based, the overall speed is not slow.

We also compare the runtime for our method and other methods. Table 5 shows that our method is significantly faster than other methods.

Table 5 Runtime (s) for different methods and models

Method	CLOP	TD	PCN	PF	Ours
Figure 4	59.66	16.65	294.00	67.38	6.27
Figure 5	10.82	6.17	78.04	13.86	1.80
Figure 6	3.89	4.91	83.69	38.98	1.89
Figure 7	2.60	5.53	28.24	70.81	0.91
Figure 8	42.85	16.24	186.30	49.99	4.66
Figure 9	60.92	155.76	317.67	81.10	7.93
Figure 10	70.58	102.41	642.01	247.77	6.37
Figure 11	103.91	40.52	241.05	68.23	28.16
Figure 12	50.58	30.01	352.99	74.68	6.98

5 Limitations

Although our method achieves good results, it still has room for improvement. Like Ref. [11], since it is a normal-based approach, it is inevitably dependent on the quality of the input normals. In each iteration of the position update, each point is estimated with reference to the direction of the normal. Therefore, inaccurate input normals may affect the filtered results. Figure 23 shows an example of such a case.

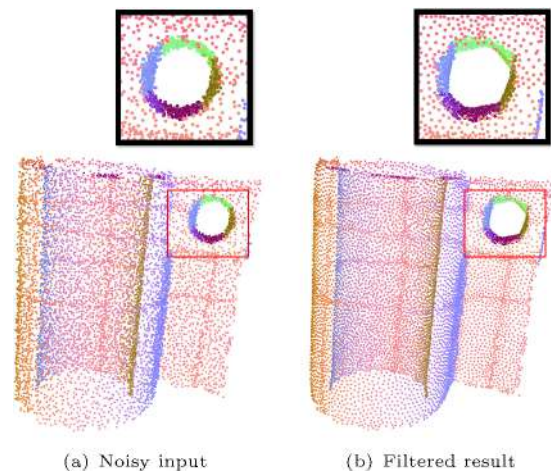


Fig. 23 An example showing poor results.

Also, like previous methods, our method may produce less desirable results when handling a very

high level of noise. For instance, Fig. 18 indicates that 1.5% noise is more challenging than the 0.5% and 1.0% noise.

In future, we hope to develop techniques to handle the above limitations.

6 Conclusions

This paper presents a method to improve point cloud filtering resulting in a more even point distribution in filtered point clouds. Built on top of Ref. [16], our method introduces a repulsion term into the objective function. It not only removes noise while preserving sharp features but also ensures a more uniform distribution of the filtered points. Experiments show that our method obtains promising filtered results under different levels of noise and for different densities. Both visual and quantitative comparisons show that it generally outperforms other existing techniques. Our method is also quicker than other compared methods.

Declaration of competing interest

The authors have no competing interests to declare that are relevant to the content of this article.

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